



# basic education

Department:  
Basic Education  
**REPUBLIC OF SOUTH AFRICA**

## **NATIONAL SENIOR CERTIFICATE**

**GRADE 12**

**MATHEMATICS P3**

**NOVEMBER 2011**

**MEMORANDUM**

**MARKS: 100**

**This memorandum consists of 14 pages.**

**NOTE:**

- If a candidate answers a question TWICE and does not delete any attempt, only mark the FIRST attempt.
- If a candidate has crossed out an attempt of a question and not redone the question, mark the crossed out version.
- Consistent Accuracy applies in ALL aspects of the marking memorandum.
- A learner cannot use what s/he must prove to prove it (i.e. the circular argument.).

**QUESTION 1**

1.1	$T_{k+1} = T_k - 2; k \geq 1; T_1 = 12$  $T_1 = 12$ $T_2 = 12 - 2 = 10$ $T_3 = 10 - 2 = 8$ $T_4 = 8 - 2 = 6$	✓ 10 ✓ 8 ✓ 6  (3)
1.2	$12 + 10 + 8 + 6 + 4 + 2 + 0 + (-2) + (-4) + (-6) + (-8) + (-10) + (-12)$ $= 0$ $\therefore$ 13 terms  <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> <p><b>Note:</b> If a learner writes out <math>12 + 10 + 8 + 6 + 4 + 2 + 0</math> then 1/3 marks</p> </div> <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> <p><b>Note:</b> Answer only: FULL marks</p> </div> <p><b>OR</b></p> <p>There are 6 positive terms before the 7th term, which is 0. We need 6 negative terms of equal value to the positive terms so that the sum is zero</p> <p>6 positive terms + 1 zero term + 6 negative terms = 13 terms</p> <p><b>OR</b></p> $\frac{n}{2}[2(12) + (n-1)(-2)] = 0$ $\frac{n}{2}[24 + 2 - 2n] = 0$ $\frac{n}{2}[26 - 2n] = 0$ $13n - n^2 = 0$ $n(13 - n) = 0$ $n \neq 0 \quad \text{or} \quad n = 13$	✓✓ expansion ✓ 13 terms  (3)  ✓ $T_7 = 0$ ✓ 12 terms ✓ 13 terms  (3)  ✓ substitution into the arithmetic sum formula  ✓ $\frac{n}{2}[26 - 2n] = 0$  ✓ 13 terms  (3) <b>[6]</b>

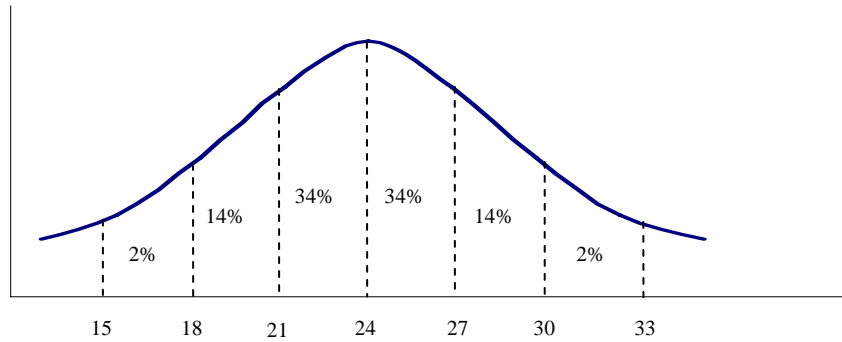
**QUESTION 2**

2.1	$42 - 28 = 14$	✓ answer (1)
2.2	Approximately 88 kg <b>NOTE:</b> Accept a range from 86 to 89 kg	✓ answer (1)
2.3	15 learners in the sample have a weight of less than 80 kg. One would expect $\frac{15}{50} \times 250 = 75$ learners in the grade to have a weight of less than 80 kg. <b>OR</b> 15 learners in the sample have a weight of less than 80 kg. One would expect $15 \times 5 = 75$ learners in the grade to have a weight of less than 80 kg. <b>NOTE:</b> <ul style="list-style-type: none"> <li>Accept <math>\frac{14}{50} \times 250 = 70</math></li> <li>Answer as percentage: 1/2 marks</li> <li>Answer only: 2/2 marks</li> </ul>	✓ Cumulative Frequency value read off the graph when less than 80 ✓ answer (2)  ✓ Cumulative Frequency value read off the graph when less than 80 ✓ answer (2)
2.4	This sampling method is biased towards those who arrive early on a Monday morning. In this way all the learners in the Grade do not have the same chance of being selected for the sample.	✓ sensible explanation of random sample (1) <b>[5]</b>

**QUESTION 3**

3.1	For mutually exclusive events $P(A \text{ or } B) = P(A) + P(B)$ $0,7 = 0,4 + k$ $k = 0,3$ <b>NOTE:</b> If the candidate writes down $k = 1 - 0,7 = 0,3$ : 0/2 marks	<b>Note:</b> Answer only: FULL marks  ✓ $0,7 = 0,4 + k$ ✓ answer (2)
3.2	For independent events $P(A \text{ and } B) = P(A) \cdot P(B)$ $= 0,4k$ $P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$ $0,7 = 0,4 + k - 0,4k$ $0,3 = 0,6k$ $k = 0,5$ <b>OR</b> $0,7 = 0,4 + k - 0,4k$ $0,3 = 0,6k$ $k = 0,5$	<b>Note:</b> <ul style="list-style-type: none"> <li>Answer only: 1/4 marks</li> <li>Wrong formula: 0/4 marks</li> </ul> ✓ $P(A \text{ and } B) = P(A) \cdot P(B)$ ✓ $0,4k$ ✓ $0,7 = 0,4 + k - 0,4k$ ✓ answer (4)  ✓✓✓ $0,7 = 0,4 + k - 0,4k$ ✓ answer (4) <b>[6]</b>

**QUESTION 4**



4.1	21 minutes is 1 standard deviation from the mean $\therefore$ 34% of the pizzas are delivered between 21 and 24 minutes  <div style="border: 1px solid black; padding: 5px; width: fit-content;"> <b>Note:</b> Answer only: FULL marks                 </div>	✓ 1 standard deviation ✓ 34%  (2)
4.2	15 minutes is 3 standard deviations to the left of the mean $\therefore$ 50% 27 minutes is 1 standard deviation to the right of the mean $\therefore$ 34% 84% of the pizzas are delivered between 15 and 27 minutes  <b>OR</b> $2\% + 14\% + 34\% + 34\%$ $= 84\%$  <div style="border: 1px solid black; padding: 5px; width: fit-content;"> <b>Note:</b>                      Answer only: FULL marks                 </div>	✓ 50% ✓ 34% ✓ 84%  ✓ 50% ✓ 34% ✓ 84%  (3)
4.3	The required 2% is the area found to the right of 2 standard deviations on the right hand side of the mean. Maximum for delivery should be $24 + 2(3)$ $= 30$ minutes  <div style="border: 1px solid black; padding: 5px; width: fit-content;"> <b>Note:</b>                      Answer only: FULL marks                 </div>	✓ 2 standard deviations ✓ $24 + 2(3)$ ✓ 30  (3) <b>[8]</b>

**QUESTION 5**

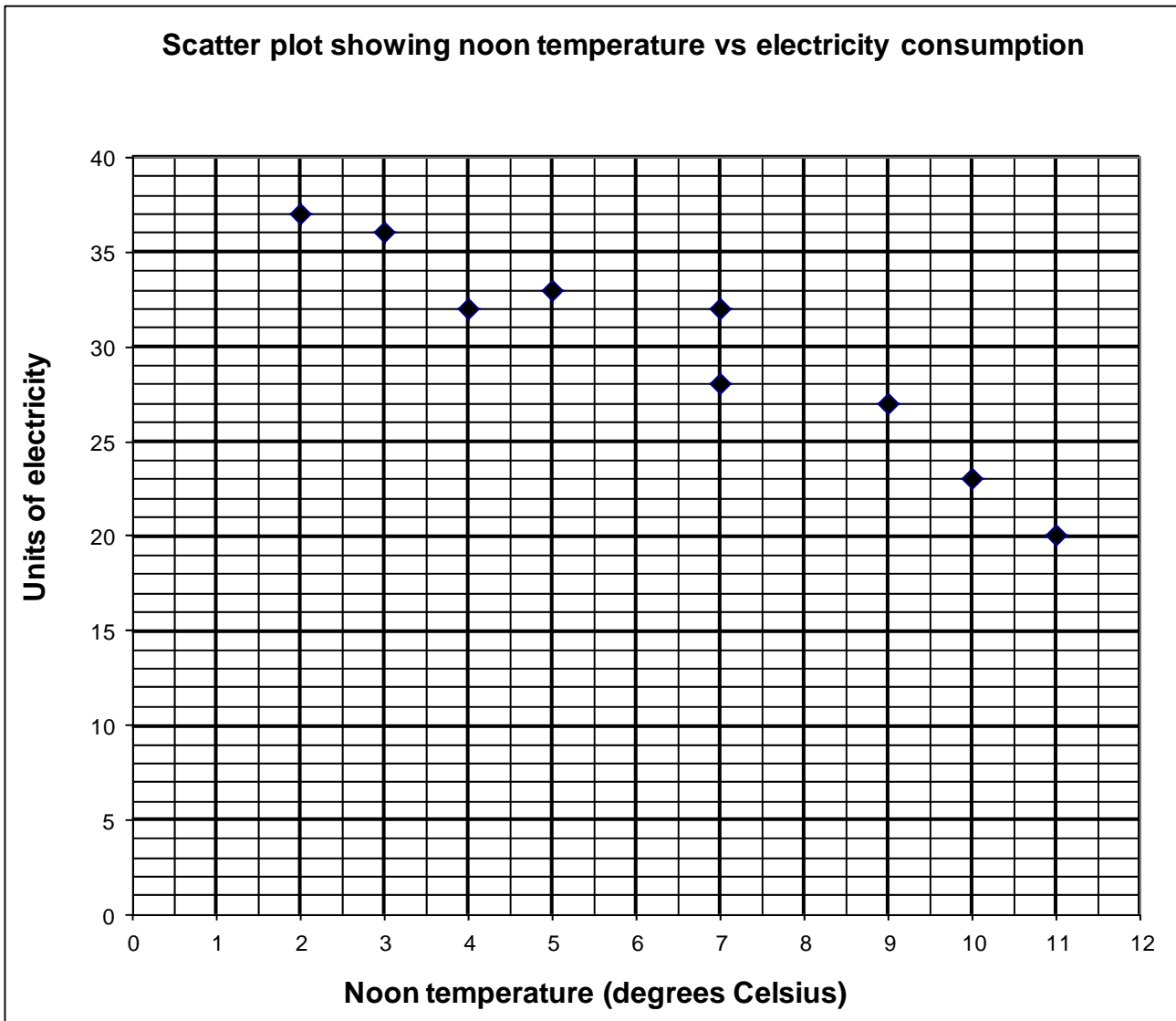
5.1	Number of unique codes $= 7 \times 7 \times 7$ $= 7^3$ $= 343$  <div style="border: 1px solid black; padding: 5px; width: fit-content;"> <b>Note:</b>                      Answer only: FULL marks                 </div>	✓ $7 \times 7 \times 7$ ✓ answer  (2)
5.2	Number of unique codes without repetition $= 7 \times 6 \times 5$ $= 210$  <b>OR</b> $\frac{7!}{4!}$ $= 210$  <div style="border: 1px solid black; padding: 5px; width: fit-content;"> <b>Note:</b>                      Answer only: FULL marks                 </div>	✓ $7 \times 6 \times 5$ ✓ answer  ✓ $\frac{7!}{4!}$ ✓ answer  (2)
5.3	Number of codes with repetition that are greater than 300 and divisible by 5 $= 4 \times 7 \times 2 - 1$ $= 55$  <b>OR</b> For a 100 numbers there are 14 numbers divisible by 5 $14 \times 4 = 56$ $56 - 1 = 55$  <div style="border: 1px solid black; padding: 5px; width: fit-content;"> <b>Note:</b> <ul style="list-style-type: none"> <li>• No CA marking for the answer.</li> <li>• Answer only 3/3 marks</li> </ul> </div>	✓ $4 \times 7 \times 2$ ✓ $- 1$ ✓ answer  ✓ $14 \times 4$ ✓ $- 1$ ✓ answer  (3) <b>[7]</b>

**QUESTION 6**

<p>6.1</p>		<p>                 ✓ <math>79 - x</math>                  ✓ 20                  ✓ <math>19 - x</math>                  ✓ 11                  ✓ 16                  ✓ <math>40 - x</math> </p> <p style="text-align: right;">(6)</p>
<p>6.2</p>	<p> <math>79 - x + 20 + x + 11 + 19 - x + 16 + 40 - x = 173</math>  <math>185 - 2x = 173</math>  <math>x = 6</math> </p> <p><b>OR</b></p> <p>232 complaints and 173 people in total                  94 complaints from 47 people                  138 complaints from remaining 126 people                  For the two to be equal  <math>126 - x = 138 - 3x</math>  <math>2x = 12</math>  <math>x = 6</math></p> <p><b>OR</b></p> <p><math>110 + 55 + 67 = 232</math>  <math>2x + 20 + 11 + 16 = 232 - 173</math>  <math>2x + 47 = 59</math>  <math>2x = 12</math>  <math>x = 6</math></p> <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> <p><b>Note:</b> Check the reasonableness of the answer.</p> </div>	<p>                 ✓ addition                  ✓ 173                  ✓ answer             </p> <p style="text-align: right;">(3)</p> <p>                 ✓ <math>126 - x</math> and <math>138 - 3x</math>                  ✓ <math>126 - x = 138 - 3x</math>                  ✓ answer             </p> <p style="text-align: right;">(3)</p> <p>                 ✓ 232                  ✓ <math>2x + 20 + 11 + 16 = 232 - 173</math>                  ✓ answer             </p> <p style="text-align: right;">(3)</p>
<p>6.3</p>	<p>                 P(at least two complaints)  <math>= \frac{11 + 20 + 6 + 16}{173}</math>  <math>= \frac{53}{173}</math>  <math>= 0,31 \quad (0,30635838\dots)</math>                  OR 30,64%             </p>	<p>                 ✓ <math>11 + 20 + 6 + 16</math>                  ✓ 173             </p> <p>                 ✓ answer             </p> <p style="text-align: right;">(3) <b>[12]</b></p>

**QUESTION 7**

<b>Noon temperature (in °C)</b>	2	3	4	5	7	7	9	10	11
<b>Units of electricity used</b>	37	36	32	33	32	28	27	23	20



7.1	<p>See scatter plot above</p> <div style="border: 1px solid black; padding: 5px; margin: 10px 0;"> <p><b>Note:</b> Please ignore the point (0 ; 41).</p> </div>	<p>✓✓✓ all 9 points plotted correctly 2 marks if 5 – 8 points are plotted correctly 1 mark if 1 – 4 points are plotted correctly.</p> <p style="text-align: right;">(3)</p>
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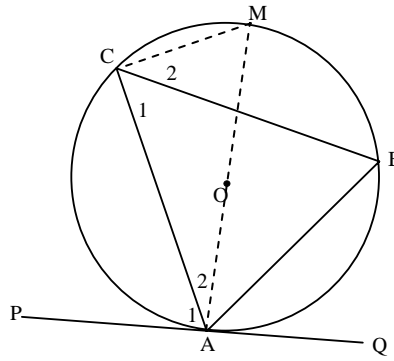
7.2	$a = 40,97$ (40,97108844...) $b = -1,74$ (-1,736394558...) $\hat{y} = 40,97 - 1,74x$ <div style="border: 1px solid black; padding: 5px; margin: 10px 0;"> <p><b>Note:</b></p> <ul style="list-style-type: none"> <li>• Penalise 1 mark for incorrect rounding to ONE decimal place in either 7.2 or 7.3</li> <li>• Answer only: FULL marks</li> </ul> </div> <p><b>NOTE:</b> If the candidate works the coefficients out manually that <math>b = \frac{-204,2}{117,6}</math> then 2 marks for <math>b</math>.</p>	✓✓ $a$ ✓ $b$ ✓ equation (4)
7.3	$r = -0,97$ (-0,9699269087...) <p><b>NOTE:</b> If the candidate gives <math>b = \frac{6,139218}{3,42928}r</math> and not simplified then 1 mark.</p>	✓✓ answer (2)
7.4	<p>There is a strong negative correlation between the noon temperature and the units of electricity used.</p> <p><b>OR</b></p> <p>As the noon temperature increases, the units of electricity used decreases.</p> <p><b>OR</b></p> <p>As the noon temperature decreases, the units of electricity used increases.</p>	✓ strong ✓ negative (2)  ✓✓ as noon temp increases & units decrease (2)  ✓✓ as noon temp decreases & units increases (2)
7.5	$\hat{y} \approx 40,97 - 1,74(8)$ $\approx 27,05$ <p><b>OR</b></p> $\hat{y} \approx 27,0799 \approx 27,08$ <div style="border: 1px solid black; padding: 5px; margin: 10px 0;"> <p><b>Note:</b></p> <ul style="list-style-type: none"> <li>• Answer only: 2/2 marks</li> <li>• Accept a range of 26,5 – 27,5 if the least squares regression line is drawn and the answer is read off: 2/2 marks</li> </ul> </div>	✓ substitution ✓ answer (2) <b>[13]</b>

**QUESTION 8**

<p>8.1</p>	<p>Draw diameter AM and join M to B.</p> <p><math>\hat{A}_1 + \hat{A}_2 = 90^\circ</math> (rad <math>\perp</math> tangent)  <math>\hat{B}_1 + \hat{B}_2 = 90^\circ</math> (<math>\angle</math>s in a semi circle)  <math>\hat{B}_2 = \hat{A}_2</math> (<math>\angle</math>s in same seg)  <math>\hat{B}_1 = \hat{A}_1</math></p> <p><b>OR</b></p> <p>Draw radii OC and OA          Let <math>\hat{A}_2 = x</math>  <math>\hat{C}_1 = x</math> (<math>\angle</math> opp = radii)  <math>\hat{A}_1 = 90^\circ - x</math> (rad <math>\perp</math> tan)  <math>\hat{AOC} = 180^\circ - 2x</math> (<math>\angle</math> sum <math>\Delta</math>)  <math>\hat{ABC} = 90^\circ - x</math> (<math>\angle</math> circ cent = 2 <math>\angle</math> circumference)  <math>\hat{ABC} = \hat{A}_1</math> (<math>= 90^\circ - x</math>)</p> <div style="border: 1px solid black; padding: 5px; margin: 10px 0;"> <p><b>NOTE:</b>              If there is no construction: 0 / 5 marks</p> <p>If candidate changes lettering and states "Similarly": full marks</p> </div> <p><b>OR</b></p> <p>Draw QA extend to P. Draw tangent CP at C.</p> <p>PC = PA (tan from comm pt)  <math>\hat{C}_2 = \hat{A}_1</math> (<math>\angle</math>s opp = sides)  <math>\hat{COA} = 2\hat{ABC}</math>          (<math>\angle</math> circ cent = 2 <math>\angle</math> circumf)  <math>\hat{A}_1 + \hat{A}_2 = 90^\circ</math> (tan <math>\perp</math> radius)  <math>\hat{COA} = 180^\circ - (90^\circ - \hat{A}_1 + 90^\circ - \hat{C}_2)</math>  <math>= \hat{A}_1 + \hat{C}_2</math>  <math>= \hat{A}_1 + \hat{A}_1</math>  <math>= 2\hat{A}_1</math>  <math>\hat{A}_1 = \frac{1}{2}\hat{COA}</math>  <math>= \hat{CBA}</math></p>	<p>✓ construction              ✓ S/R              ✓ <math>\hat{B}_1 + \hat{B}_2 = 90^\circ</math>              ✓ <math>\angle</math>s in a semi circle              ✓ S/R</p> <p>(5)</p> <p>✓ construction              ✓ <math>\hat{A}_1 = 90^\circ - x</math>              ✓ rad <math>\perp</math> tan              ✓ S/R              ✓ S/R</p> <p>(5)</p> <p>✓ construction              ✓ S/R              ✓ S/R              ✓ <math>\hat{A}_1 + \hat{A}_2 = 90^\circ</math>              ✓ tan <math>\perp</math> radius</p> <p>(5)</p>
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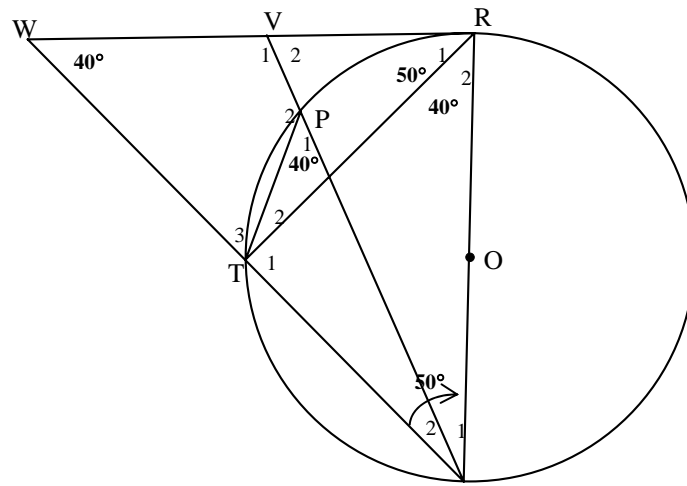
Draw diameter AM and Join M and C  
 $\widehat{MCA} = 90^\circ$  ( $\angle$ s in semi circle)  
 $\widehat{AMC} + \widehat{A}_2 = 90^\circ$  ( $\angle$  sum  $\Delta$ )  
 $\widehat{A}_1 + \widehat{A}_2 = 90^\circ$  (rad  $\perp$  tangent)  
 $\widehat{AMC} = \widehat{A}_1$   
 $\widehat{AMC} = \widehat{B}$  ( $\angle$ s in same seg)  
 $\widehat{A}_1 = \widehat{B}$



✓ construction  
 ✓ S/R  
 ✓ S/R

✓  $\widehat{A}_1 + \widehat{A}_2 = 90^\circ$   
 ✓ tan  $\perp$  radius

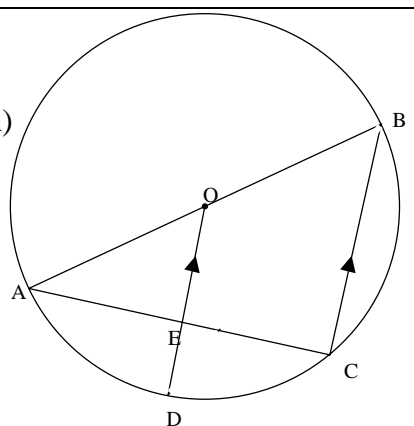
(5)



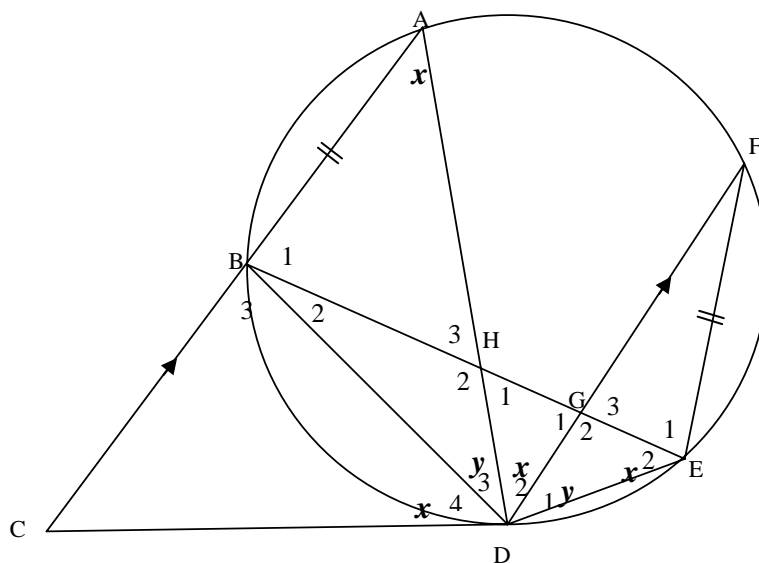
8.2.1	$\widehat{WRS} = 90^\circ$ (tan $\perp$ radius)	✓ statement (1)
8.2.2	$\widehat{RST} = 50^\circ$ (tan ch th) $\widehat{W} = 40^\circ$ ( $\angle$ sum $\Delta$ ) <b>OR</b> $\widehat{T}_1 = 90^\circ$ ( $\angle$ s in semi circle) $\widehat{W} + \widehat{R}_1 = \widehat{T}_1$ (ext $\angle$ $\Delta$ ) $\widehat{W} = 40^\circ$	✓ S/R ✓ $\widehat{W} = 40^\circ$ ✓ $\widehat{W} + \widehat{R}_1 = \widehat{T}_1$ ✓ $\widehat{W} = 40^\circ$ (2)
8.2.3	$\widehat{R}_2 = 40^\circ$ (tan $\perp$ radius) $\widehat{P}_1 = 40^\circ$ ( $\angle$ s in same seg)	✓ $\widehat{R}_2 = 40^\circ$ ✓ $\widehat{P}_1 = 40^\circ$ ✓ $\angle$ s in same seg (3)

<p>8.2.4 <math>\hat{P}_1 = \hat{W}</math> (<math>= 40^\circ</math>)                  WVPT is a cyclic quadrilateral (ext <math>\angle =</math> int opp)  <math>\hat{V}_1 = \hat{P}\hat{T}\hat{S}</math> (ext <math>\angle</math> cyclic quad)</p> <p><b>OR</b>  <math>\hat{T}_1 = 90^\circ</math> (<math>\angle</math>s in semi circle)  <math>\hat{P}\hat{T}\hat{S} = 90^\circ + \hat{T}_2</math>  <math>\hat{T}_2 = \hat{S}_1</math> (<math>\angle</math>s in same seg)  <math>\hat{P}\hat{T}\hat{S} = 90^\circ + \hat{S}_1</math>  <math>\hat{V}_1 = 90^\circ + \hat{S}_1</math> (ext <math>\angle</math> <math>\Delta</math>)  <math>\hat{V}_1 = \hat{P}\hat{T}\hat{S}</math></p> <p><b>OR</b>  <math>\hat{P}_2 = 140^\circ</math> (<math>\angle</math>s on str line)  <math>\hat{W} + \hat{P}_2 = 180^\circ</math>                  WVPT is cyclic quad (opp <math>\angle</math>s suppl)  <math>\hat{V}_1 = \hat{P}\hat{T}\hat{S}</math> (ext <math>\angle</math> cyclic quad)</p> <p><b>OR</b>  <math>\hat{V}_1 = \hat{R}_1 + \hat{R}_2 + \hat{S}_1</math> (ext <math>\angle</math> <math>\Delta</math>)  <math>\hat{V}_1 = 90^\circ + \hat{S}_1</math>  <math>\hat{P}\hat{T}\hat{S} = 90^\circ + \hat{T}_2</math>                  But <math>\hat{T}_2 = \hat{S}_1</math> (<math>\angle</math>s in same seg)  <math>\hat{V}_1 = \hat{P}\hat{T}\hat{S}</math></p> <p><b>OR</b>                  In <math>\Delta</math>PTS and <math>\Delta</math>WVS  <math>\hat{P}_1 = \hat{W}</math> (<math>= 40^\circ</math>)  <math>\hat{S}_2</math> is common  <math>\hat{V}_1 = \hat{P}\hat{T}\hat{S}</math> (<math>\angle</math> sum <math>\Delta</math>)</p>	<p>✓ <math>\hat{P}_1 = \hat{W}</math>                  ✓ WVPT is a cyclic quadrilateral                  ✓ ext <math>\angle =</math> in opp                  ✓ ext <math>\angle</math> cyclic quad (4)</p> <p>✓ <math>\angle</math>s in semi circle                  ✓ <math>\hat{P}\hat{T}\hat{S} = 90^\circ + \hat{T}_2</math>                  ✓ <math>\hat{T}_2 = \hat{S}_1</math>                  ✓ <math>\angle</math>s in same seg (4)</p> <p>✓ <math>\hat{W} + \hat{P}_2 = 180^\circ</math>                  ✓ WVPT is a cyclic quadrilateral                  ✓ opp <math>\angle</math> suppl                  ✓ ext <math>\angle</math> cyclic quad (4)</p> <p>✓ <math>\hat{V}_1 = 90^\circ + \hat{S}_1</math>                  ✓ <math>\hat{P}\hat{T}\hat{S} = 90^\circ + \hat{T}_2</math>                  ✓ <math>\hat{T}_2 = \hat{S}_1</math>                  ✓ <math>\angle</math>s in same seg (4)</p> <p>✓ identification of triangles                  ✓ <math>\hat{P}_1 = \hat{W}</math>                  ✓ <math>\hat{S}_2</math> is common                  ✓ <math>\angle</math> sum <math>\Delta</math> (4)</p> <p style="text-align: right;"><b>[15]</b></p>
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**QUESTION 9**

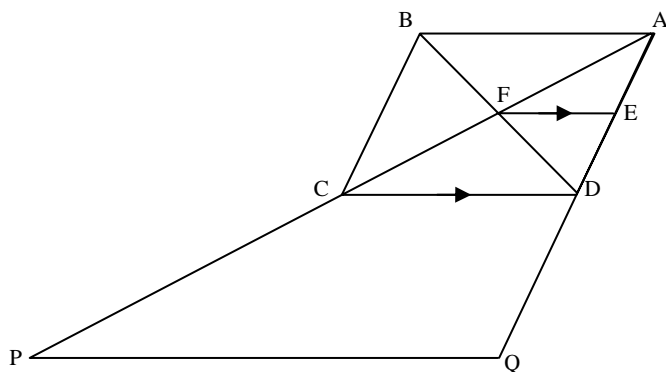
<p>9.</p>	<p> <math>\hat{C} = 90^\circ</math> (<math>\angle</math>s in semi circle)  <math>\hat{OEA} = 90^\circ</math> (corres <math>\angle</math>s; <math>OD \parallel BC</math>)  <math>AE = 8 \text{ cm}</math> (line from circ cent <math>\perp</math> ch bis ch)  <math>OE = 6 \text{ cm}</math> (Pythagoras)  <math>ED = 10 - 6 = 4 \text{ cm}</math> </p> <p><b>OR</b></p> <p> <math>\hat{C} = 90^\circ</math> (<math>\angle</math>s in semi circle)  <math>\hat{OEA} = 90^\circ</math> (corres <math>\angle</math>s; <math>OD \parallel BC</math>)  <math>OE \parallel BC</math> (given)  <math>OA = OB</math> (radii)  <math>AE = EC = 8 \text{ cm}</math> (midpoint theorem)  <math>OE = 6 \text{ cm}</math> (Pythagoras)  <math>ED = 10 - 6 = 4 \text{ cm}</math> </p> <p><b>OR</b></p> <p> <math>\hat{C} = 90^\circ</math> (<math>\angle</math>s in semi circle)  <math>BC^2 = (20)^2 - (16)^2</math>  <math>BC^2 = 144</math>  <math>BC = 12</math>  <math>OE = \frac{1}{2} BC</math> (midpoint theorem)  <math>OE = 6 \text{ cm}</math>  <math>OD = 10 \text{ cm}</math>  <math>ED = 10 - 6 = 4 \text{ cm}</math> </p> <p><b>OR</b></p> <p> <math>\hat{C} = 90^\circ</math> (<math>\angle</math>s in semi circle)  <math>BC^2 = (20)^2 - (16)^2</math>  <math>BC^2 = 144</math>  <math>BC = 12</math>  <math>OE = \frac{1}{2} BC</math> (midpoint theorem)  <math>OE = 6 \text{ cm}</math>  <math>ED = 4 \text{ cm}</math> </p>		<p> <math>\checkmark \hat{C} = 90^\circ</math>  <math>\checkmark \hat{OEA} = 90^\circ</math>  <math>\checkmark</math> line from circ cent <math>\perp</math> ch bis ch  <math>\checkmark OE = 6 \text{ cm}</math>  <math>\checkmark ED = 4 \text{ cm}</math> </p> <p> <math>\checkmark \hat{C} = 90^\circ</math>  <math>\checkmark \hat{OEA} = 90^\circ</math>  <math>\checkmark</math> midpoint theorem  <math>\checkmark OE = 6 \text{ cm}</math>  <math>\checkmark ED = 4 \text{ cm}</math> </p> <p> <math>\checkmark \hat{C} = 90^\circ</math>  <math>\checkmark BC = 12</math>  <math>\checkmark</math> reason  <math>\checkmark OE = 6 \text{ cm}</math>  <math>\checkmark ED = 4 \text{ cm}</math> </p> <p style="text-align: right;"><b>[5]</b></p> <p> <math>\checkmark \hat{C} = 90^\circ</math>  <math>\checkmark BC = 12</math>  <math>\checkmark</math> reason         </p> <p> <math>\checkmark OE = 6 \text{ cm}</math>  <math>\checkmark ED = 4 \text{ cm}</math> </p> <p style="text-align: right;"><b>[5]</b></p>
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**QUESTION 10**



10.1	$\hat{A} = \hat{D}_4 = x$ (tan ch th) $\hat{E}_2 = x$ (tan ch th) <b>OR</b> ( $\angle$ s in same seg) $\hat{D}_2 = \hat{A} = x$ (alt $\angle$ s; CA $\parallel$ DF)	✓ $\hat{A} = x$ ✓ tan ch th ✓ $\hat{E}_2 = x$ ✓ reason ✓ $\hat{D}_2 = x$ ✓ alt $\angle$ s; CA $\parallel$ DF (6)
10.2	In $\triangle BHD$ and $\triangle FED$ 1. $\hat{B}_2 = \hat{F}$ ( $\angle$ s in same seg) 2. $\hat{D}_3 = \hat{D}_1$ (= chs subt = $\angle$ s)  $\triangle BHD \parallel \triangle FED$ ( $\angle\angle\angle$ )	✓ $\hat{B}_2 = \hat{F}$ ✓ $\angle$ s in same seg ✓ $\hat{D}_3 = \hat{D}_1$ ✓ = chs subt = $\angle$ s ✓ $\angle\angle\angle$ (5)
10.3	$\frac{FE}{BH} = \frac{FD}{BD}$ ( $\parallel \Delta$ s) But $FE = AB$ (given) $\frac{AB}{BH} = \frac{FD}{BD}$ $AB \cdot BD = FD \cdot BH$	✓ $\frac{FE}{BH} = \frac{FD}{BD}$ ✓ $FE = AB$ (2)  <b>[13]</b>

**QUESTION 11**



11.1	$AF = FC$ $FE \parallel CD$ $AE = ED$ (diags of parallelogram bisect) (Prop Th; $FE \parallel CD$ ) <b>OR</b> (Midpoint Theorem)	✓ $AF = FC$ ✓ reason (2)
11.2	$\frac{AC}{CP} = \frac{1}{2}$ (given) $\frac{AD}{DQ} = \frac{1}{2}$ (given) $\frac{AC}{CP} = \frac{AD}{DQ}$ $CD \parallel PQ$ (converse proportionality theorem) $CD \parallel FE$ (given) $\therefore PQ \parallel FE$ <b>OR</b> $\frac{AC}{AP} = \frac{1}{3}$ $\frac{AD}{AQ} = \frac{1}{3}$ $\frac{AC}{AP} = \frac{AD}{AQ}$ $CD \parallel PQ$ (converse proportionality theorem) $CD \parallel FE$ (given) $\therefore PQ \parallel FE$ <b>OR</b> $\frac{AF}{AP} = \frac{1}{6}$ $\frac{AE}{AQ} = \frac{1}{6}$ $\frac{AF}{AP} = \frac{AE}{AQ}$ $\therefore PQ \parallel FE$ (converse proportionality theorem)	✓ ratios equal ✓ $CD \parallel PQ$ ✓ reason: <b>converse</b> prop th and conclusion (3)  ✓ ratios equal ✓ $CD \parallel PQ$ ✓ reason: <b>converse</b> prop th and conclusion (3)  ✓ $\frac{AF}{AP} = \frac{1}{6}$  ✓ $\frac{AF}{AP} = \frac{AE}{AQ}$ ✓ conv prop theorem

<p>11.3</p>	<p>In <math>\triangle AEF</math> and <math>\triangle APQ</math></p> <ol style="list-style-type: none"> <li><math>\hat{A}</math> is common</li> <li><math>\hat{A}\hat{E}F = \hat{A}\hat{Q}P</math> (corres <math>\angle</math>s; <math>FE \parallel PQ</math>)</li> <li><math>\hat{A}\hat{F}E = \hat{A}\hat{P}Q</math> (corres <math>\angle</math>s; <math>FE \parallel PQ</math>)</li> </ol> <p><math>\therefore \triangle AEF \parallel \triangle APQ</math> (<math>\angle\angle\angle</math>)</p> $\frac{FE}{PQ} = \frac{AF}{AP} \quad (\parallel \Delta\text{s})$ $\frac{FE}{60} = \frac{1}{6}$ <p><math>FE = 10</math> cm</p> <p><b>OR</b></p> <p>In <math>\triangle ADC</math> and <math>\triangle APQ</math></p> <ol style="list-style-type: none"> <li><math>\hat{A}</math> is common</li> <li><math>\hat{A}\hat{D}C = \hat{A}\hat{Q}P</math> (corres <math>\angle</math>s; <math>CD \parallel PQ</math>)</li> <li><math>\hat{A}\hat{C}D = \hat{A}\hat{P}Q</math> (corres <math>\angle</math>s; <math>CD \parallel PQ</math>)</li> </ol> <p><math>\therefore \triangle ADC \parallel \triangle APQ</math> (<math>\angle\angle\angle</math>)</p> $\frac{AC}{AP} = \frac{AD}{AQ} = \frac{1}{3} \quad (\parallel \Delta\text{s})$ $CD = \frac{1}{3} PQ$ <p><math>CD = 20</math> cm But <math>AF = FC</math> <math>AE = ED</math> (Midpoint Theorem)</p> $FE = \frac{1}{2} CD$ <p><math>FE = 10</math> cm</p> <div style="border: 1px solid black; padding: 5px; width: fit-content; margin: 10px auto;"> <p><b>NOTE:</b> If the similarity has not been proven, then max 3/5 marks</p> </div>	<p>✓ first pair of angles equal with reason ✓ second pair of angles equal with reason</p> <p>✓ <math>\frac{AF}{AP} = \frac{1}{6}</math> ✓ <math>\frac{FE}{PQ} = \frac{AF}{AP}</math> ✓ answer (5)</p> <p>✓ first pair of angles equal with reason ✓ second pair of angles equal with reason</p> <p>✓ <math>CD = \frac{1}{3} PQ</math></p> <p>✓ <math>FE = \frac{1}{2} CD</math> ✓ answer (5)</p> <p style="text-align: right;"><b>[10]</b></p>
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**TOTAL: 100**